

1 **APPENDIX A.**

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3 The following text is a description of the steps needed to estimate reference evapotranspiration for a 0.12
4 m tall reference surface using daily weather data as adopted by the American Society of Civil Engineers
5 (Allen et al., 2005).

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7 STEP 1: Extraterrestrial radiation (R_a) is calculated for each day using the following equations from
8 Duffie and Beckman (1980).

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10 $G_{SC} = 0.082 \text{ MJ m}^{-2} \text{ min}^{-1} = \text{solar constant}$

11 $\sigma = 4.90 \times 10^{-9} \text{ MJ m}^{-2} \text{ d}^{-1} \text{ K}^{-4} = \text{Steffan-Boltzman constant}$

12 $\phi = \frac{\pi L}{180} = \text{latitude in radians converted from latitude } (L) \text{ in degrees}$

13 $d_r = 1 + 0.033 \cos\left(\frac{2\pi}{365} i\right) = \text{correction for eccentricity on day } i \text{ of the year}$

14 $\delta = 0.409 \sin\left(\frac{2\pi}{365} i - 1.39\right) = \text{declination of the sun in radians on day } i \text{ of the year}$

15 $\omega_s = \cos^{-1}[-\tan \phi \tan \delta] = \text{sunrise hour angle in radians}$

16 $R_a = \left(\frac{24 \cdot 60}{\pi}\right) G_{SC} d_r [\omega_s \sin \delta \sin \phi + \cos \phi \cos \delta \sin \omega_s] = \text{extraterrestrial rad. (MJ m}^{-2} \text{ d}^{-1})$

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18 STEP 2: Calculate the daily net radiation (R_n) expected over grass in $\text{MJ m}^{-2} \text{ d}^{-1}$ using equations from
19 Allen et al. (1994).

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21 $R_{so} = R_a (0.75 + 2.0 \times 10^{-5} E_l) = \text{clear sky total global solar radiation in MJ m}^{-2} \text{ d}^{-1}$

22 $R_{ns} = (1 - 0.23) R_s = \text{net solar radiation for measured solar radiation } (R_s) \text{ in MJ m}^{-2} \text{ d}^{-1}$

1 $f = 1.35 \frac{R_s}{R_{so}} - 0.35$ = a cloudiness function of R_s and R_{so}

2 For maximum daily air temperature (T_x) and minimum daily air temperature (T_n) in °C,

3 $e_s(T_x) = 0.6108 \exp\left(\frac{17.27T_x}{T_x + 237.3}\right)$ = saturation vapor pressure (kPa)

4 $e_s(T_n) = 0.6108 \exp\left(\frac{17.27T_n}{T_n + 237.3}\right)$ = saturation vapor pressure (kPa)

5 For maximum relative humidity (RH_x) and minimum relative humidity (RH_n) in (%),

6 $e_a = \frac{e_s(T_x) \frac{RH_n}{100} + e_s(T_n) \frac{RH_x}{100}}{2}$ = actual vapor pressure (kPa)

7 For daily mean dew point temperature (T_d) in °C,

8 $e_a = 0.6108 \exp\left[\frac{17.27T_d}{T_d + 237.3}\right]$ = actual vapor pressure (kPa)

9 $\varepsilon' = 0.34 - 0.14\sqrt{e_a}$ = apparent 'net' clear sky emissivity

10 $R_{nl} = -f \varepsilon' \sigma \left[\frac{(T_x + 273.15)^4 + (T_n + 273.15)^4}{2} \right]$ = net long wave radiation in MJ m⁻² d⁻¹

11 $R_n = R_{ns} + R_{nl}$ = net radiation over grass in MJ m⁻² d⁻¹

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13 STEP 3: Calculate variables needed to compute ET_h , ET_o and ET_r .

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15 For elevation (E_L) in meters,

16 $\beta = 101.3 \left(\frac{293 - 0.0065E_L}{293} \right)^{5.26}$ = barometric pressure (kPa)

17 $\lambda = 2.45$ = latent heat of vaporization in (MJ kg⁻¹)

18 $\gamma = 0.00163 \frac{\beta}{\lambda}$ = psychrometric constant in kPa °C⁻¹

1 $T_m = \frac{T_x + T_n}{2}$ = mean daily temperature in °C

2 $e^o = 0.6108 \exp\left(\frac{17.27T_m}{T_m + 237.3}\right)$ = saturation vapor pressure (kPa) at T_m

3 $\Delta = \frac{4099e^o}{(T_m + 237.3)^2}$ = slope of the saturation vapor pressure curve (kPa °C⁻¹)

4 $G \approx 0$ = soil heat flux density in MJ m⁻² d⁻¹

5 $e_s = \frac{e_s(T_x) + e_s(T_n)}{2}$ = mean daily saturation vapor pressure (kPa)

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7 STEP 4: Calculate ET_o using the ASCE-EWRI standardized equation for short canopy reference ET

8 (Allen et al., 2005)

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10 For U_2 the wind speed at 2 m height and temperature and relative humidity measured between 1.5 and

11 2.0 m height,

12 $R_o = \frac{0.408\Delta(R_n - G)}{\Delta + \gamma(1 + 0.34U_2)}$ = radiation term (mm d⁻¹)

13 $A_o = \frac{\left(\frac{900\gamma}{T_M + 273}\right)U_2(e_s - e_a)}{\Delta + \gamma(1 + 0.34U_2)}$ = aerodynamic term (mm d⁻¹)

14 $ET_o = R_o + A_o$ = Standardized Reference Evapotranspiration for short canopies (mm d⁻¹)